

## A New Method for Measuring 1:1 Association Constants Based on Releasing Rate of Free Ligand from Aqueous into Gaseous Phase, Applied to Determining Formation Constants of Metal Acetylacetonate Complexes

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A simple method is presented that allows estimation of 1:1 association constants between volatile and nonvolatile solutes in aqueous medium. On introducing an inert gas at a constant flow rate into the aqueous phase, the volatile solute is expelled from the solution, and the amount of the released solute is measured as a function of aeration time. Measurements are made in two separate runs at the same inert gas flow rate, one in the absence and the other in the presence of nonvolatile solutes. The releasing rate of the volatile solute is reduced with increasing association between both the solutes in the aqueous medium. The method was used to estimate formation constants of 1:1 acetylacetonate complexes with metal ions, Cu(II), Ni(II), Co(II), Mg(II), Fe(II), Fe(III), and Al(III), at 25.0 °C and  $I=0.1$  (NaClO<sub>4</sub>), results being compared with literature values.

It has been shown that the disproportionation constant of mercury(I) in aqueous medium, i.e., the equilibrium constant for  $\text{Hg}_2^{2+} \rightleftharpoons \text{Hg}^{2+} + \text{Hg}$ , can be determined by combining two rate constants obtained from two independent experiments: one is concerned with measurement of the disproportionation rate while the equilibrium is caused to shift to the right by introducing nitrogen gas at a constant flow rate into the solution containing Hg(I) to expel Hg, and the other is concerned with measurement of the releasing rate of metallic mercury in the absence of Hg(II) at the same N<sub>2</sub> gas flow rate.<sup>1)</sup> The present work was undertaken to demonstrate that the method might be applicable widely to systems where association occurs in aqueous medium between volatile and nonvolatile solutes.

In this work we are concerned with measurement of 1:1 formation constants of metal complexes. Acetylacetonate was selected because this ligand is volatile<sup>2)</sup> and because formation constants for a wide variety of metal ions are available from published compilations.<sup>3)</sup> Various methods such as spectrophotometry, potentiometry, polarography, calorimetry, and solvent extraction have so far been used to determine formation constants for metal acetylacetonates.<sup>3–8)</sup> Compared with these techniques, the present method is simple and not specific for the metal ions to be studied.

### Experimental

**Reagents and Materials.** Distilled deionized water was used throughout. Acetylacetonate was of analytical reagent grade from Wako Pure Chemical. Stock solutions of 0.1 or 0.2 M (1 M=1 mol dm<sup>-3</sup>) metal ions were prepared by dissolving their salts (ammonium iron(III) sulfate, aluminum potassium sulfate, sulfate and chloride for Cu(II), and

chlorides for the other metals) in 0.01 M HClO<sub>4</sub>, and standardizing gravimetrically (Fe: Fe<sub>2</sub>O<sub>3</sub> converted to hydroxide; Al: 8-quinolinolate; Ni: dimethylglyoximate; Co: Co<sub>3</sub>O<sub>4</sub> converted to  $\alpha$ -nitroso- $\beta$ -naphtholate) or titrimetrically (Mg: EDTA; Cu: iodometry). Amberlite XAD-2 resin, 20–50 mesh (Rohm and Hass), was ground in an agate mortar, a 50–80 mesh portion was collected and washed with ethanol by decantation until the supernatant became clear.

**Preparation of Sample Solutions.** A known amount of acetylacetonate (5 to 50  $\mu\text{L}$ ) was added with a 25 or 100  $\mu\text{L}$  micropipet to ca. 50 cm<sup>3</sup> of 0.1 M NaClO<sub>4</sub>, a known volume of a metal ion stock solution was added, the pH was adjusted with a suitable buffer solution, and finally the solution was diluted to 100 cm<sup>3</sup> with 0.1 M NaClO<sub>4</sub> (the acetylacetonate concentration was in the range of  $4.87 \times 10^{-4}$  to  $4.87 \times 10^{-3}$  M and the metal ion concentration was in the range indicated in Tables 1–3). The buffer solutions used are as follows: 0.2 M acetic acid–0.2 M sodium acetate (pH=3–6), 0.1 M sodium dihydrogenphosphate–0.1 M sodium hydroxide (pH=6–7.5), and 0.2 M boric acid–0.2 M potassium chloride–0.2 M sodium hydroxide (pH=7.5–10). For pHs lower than 3, perchloric acid (0.1 M) was used. The amount of the buffer or HClO<sub>4</sub> solution added to an aqueous solution containing both acetylacetonate and metal ion was moderated so that the contribution of buffer salts to the increase in ionic strength was less than 0.01. The pH was measured with a Horiba Type F-7 pH meter to 0.01 pH unit.

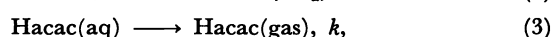
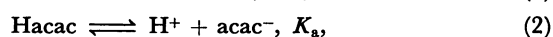
**Apparatus and Procedures.** A 25 cm<sup>3</sup> portion of sample solution was transferred into a 100 cm<sup>3</sup> Erlenmeyer flask with a ground glass joint, the flask being immersed in a thermostated bath at  $25.0 \pm 0.1$  °C. A gas-inlet-type adaptor was mounted on the flask and nitrogen gas was dispersed through the solution via a sintered glass ball at a constant flow rate of 895 cm<sup>3</sup> min<sup>-1</sup>. The N<sub>2</sub> gas flow rate was adjusted by means of a needle valve and monitored during the aeration by a flow meter (Ueshima Brooks Rotameter); a deviation within 2% was observed around the adopted flow rate. The N<sub>2</sub> gas leaving the sample solution was

passed through a 5 mm×5 cm glass column which contained XAD-2 resin beads 3.5 cm in length and had its exit end plugged with glass wool. After a fixed time, the N<sub>2</sub> gas stream was interrupted, the XAD column was replaced by another one, and the introduction of N<sub>2</sub> gas was resumed. This operation was repeated at regular time intervals. The acetylacetone adsorbed on the resin was completely eluted out with a 5 cm<sup>3</sup> ethanol, and the amount expelled from the solution during the fixed time was determined spectrophotometrically at 272 nm by reference to a calibration curve prepared in advance with acetylacetone-ethanol solutions of known concentrations. The XAD column, after subjected to elution with ethanol and air-dried, could be used repeatedly.

After completion of each aeration run, the pH of the sample solution was checked; no appreciable change in pH was found before and after aeration.

## Results

**Derivation of an Equation That Allows Estimation of 1:1 Metal Acetylacetonate Complex Formation Constants.** The equilibria among the species that should be taken into account are



where  $K_1$  is the formation constant of 1:1 metal acetylacetonate complex,  $K_a$  is the acid dissociation constant of acetylacetone (Hacac), and  $k$  is the rate constant for the expulsion of Hacac molecules from the aqueous into the gaseous phase. For convenience, symbol L<sup>-</sup> will hereafter be used to denote species acac<sup>-</sup>.

The solute HL expelled into the gaseous phase is to be trapped successively by XAD-2 columns, and the amount,  $Q_{\text{HL}}$ , trapped during a fixed time is measured as a function of aeration time,  $t$ . Here, we assume that the releasing rate of HL at a constant N<sub>2</sub> gas flow rate is of first-order dependence on the concentration of this species present in the solution, and thus

$$dQ_{\text{HL}}V^{-1}/dt = k[\text{HL}], \quad (4)$$

where  $V$  is the volume of the aqueous phase. We have mass-balance equations

$$C_M = [\text{M}^{n+}] + [\text{ML}^{n-1}], \quad (5)$$

$$\begin{aligned} C_{\text{HL}} &= [\text{HL}] + Q_{\text{HL}}V^{-1} + [\text{ML}^{n-1}] + [\text{L}^-] \\ &= [\text{HL}] + Q_{\text{HL}}V^{-1} + K_1[\text{L}^-][\text{M}^{n+}] + [\text{L}^-] \\ &= [\text{HL}] + Q_{\text{HL}}V^{-1} + (K_1[\text{M}^{n+}] + 1)K_a[\text{HL}][\text{H}^+]^{-1}, \end{aligned} \quad (6)$$

where  $C_M$  and  $C_{\text{HL}}$  indicate the total concentration of metal ions and that of acetylacetone, respectively. Substitution of Eq. 6 into Eq. 4 yields

$$dQ_{\text{HL}}V^{-1}/dt = k(C_{\text{HL}} - Q_{\text{HL}}V^{-1})/(1 + K_a[\text{H}^+]^{-1} + K_1K_a[\text{M}^{n+}][\text{H}^+]^{-1}), \quad (7)$$

which becomes, on integration and with  $Q_{\text{HL}}=0$  at  $t=0$ ,

$$\ln(C_{\text{HL}} - Q_{\text{HL}}V^{-1}) = -kt/(1 + K_a[\text{H}^+]^{-1} + K_1K_a[\text{M}^{n+}][\text{H}^+]^{-1}) + \ln C_{\text{HL}}. \quad (8)$$

Plots of  $\ln(C_{\text{HL}} - Q_{\text{HL}}V^{-1})$  vs.  $t$  will give a straight line with a slope which corresponds to  $-k/(1 + K_a[\text{H}^+]^{-1} + K_1K_a[\text{M}^{n+}][\text{H}^+]^{-1})$  or to  $-k/(1 + K_a[\text{H}^+]^{-1})$  in the absence of metal ions. Under the condition that the total concentration of metal ions is sufficiently large compared to the concentration of the metal complex formed, that is,  $C_M \gg [\text{ML}^{n-1}]$ , we can set  $[\text{M}^{n+}]$  in Eq. 8 equal to  $C_M$ .

**Estimation of  $k$  and  $K_a$ .** The constants  $k$  and  $K_a$  were determined from runs in the absence of metal ions. Figure 1 shows some plots constructed with the aid of Eq. 8. It is found that these plots give straight lines up to ca. 70% release of the acetylacetone initially present in the solution. This linearity verifies the validity of the assumption that the releasing rate of HL is first order in this species at a constant aeration rate. It can be seen from Fig. 1 that when the total concentration of HL is the same, the

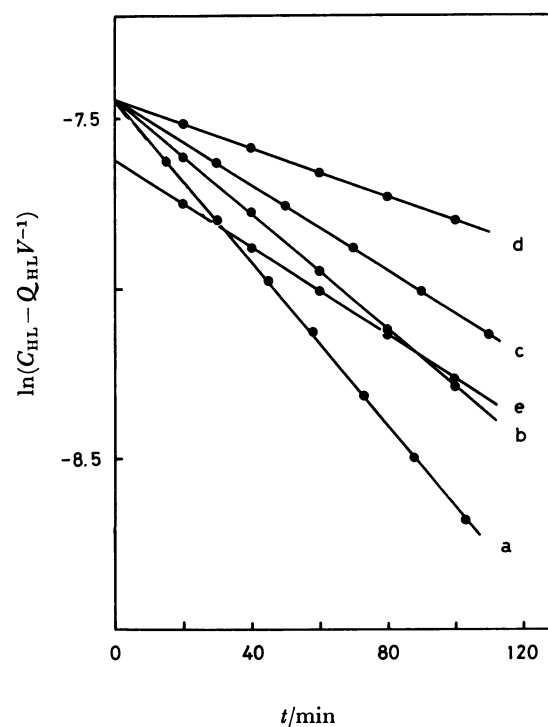


Fig. 1. The plots of  $\ln(C_{\text{HL}} - Q_{\text{HL}}V^{-1})$  vs.  $t$  in the absence of metal ions. pH 2.30; N<sub>2</sub> gas flow rate: (a) 895, (b) 640, (c) 460, (d) 255, (e) 460 cm<sup>3</sup> min<sup>-1</sup>;  $C_{\text{HL}}$ : (a)–(d)  $5.85 \times 10^{-4}$ , (e)  $4.87 \times 10^{-4}$  mol dm<sup>-3</sup>.

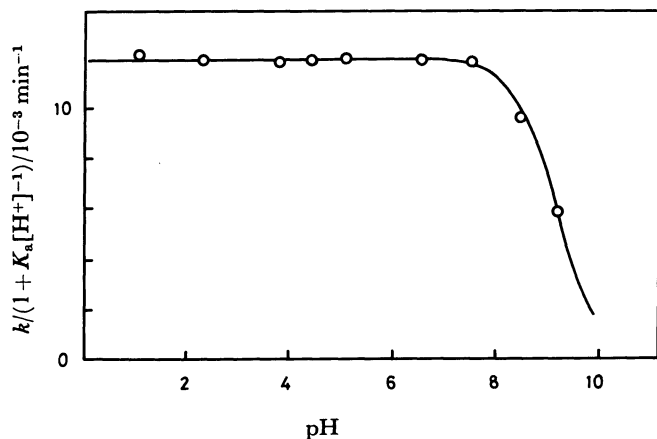


Fig. 2. The plots of  $k/(1 + K_a[H^+]^{-1})$  vs. pH in the absence of metal ions.  $N_2$  gas flow rate  $895 \text{ cm}^3 \text{ min}^{-1}$ ;  $C_{HL} = 5.85 \times 10^{-4} \text{ mol dm}^{-3}$ . The curve calculated using  $k = 1.20 \times 10^{-2} \text{ min}^{-1}$  and  $pK_a = 9.17$  is depicted in a solid line.

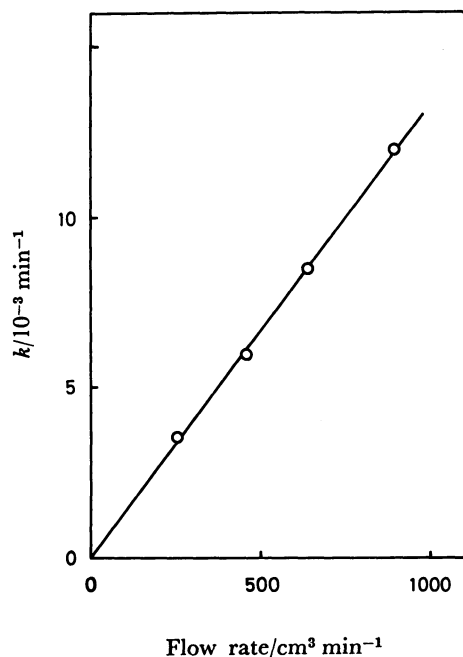


Fig. 3.  $k$  as a function of  $N_2$  gas flow rate in the absence of metal ions. pH 2.30;  $C_{HL} = 5.87 \times 10^{-4} \text{ mol dm}^{-3}$ .

slopes coincide with one another at the same aeration rate. This also supports the validity of Eq. 4.

At a constant  $N_2$  gas flow rate, the slope of the straight line is almost constant in the acidic region, but steeply decreases in higher pH solutions, as seen from the plots of  $k/(1 + K_a[H^+]^{-1})$  vs. pH shown in Fig. 2. A least-squares calculation has revealed that  $k$  is  $1.20 \times 10^{-2} \text{ min}^{-1}$  at an aeration rate of  $895 \text{ cm}^3 \text{ min}^{-1}$  and that  $pK_a$  is 9.17. The  $K_a$  value thus determined is about half the reference one, 8.82 as  $pK_a$ ,<sup>9</sup> reported at  $25^\circ \text{C}$  and  $I = 0.1(\text{Na}^+, \text{H}^+)\text{ClO}_4$ . The rate

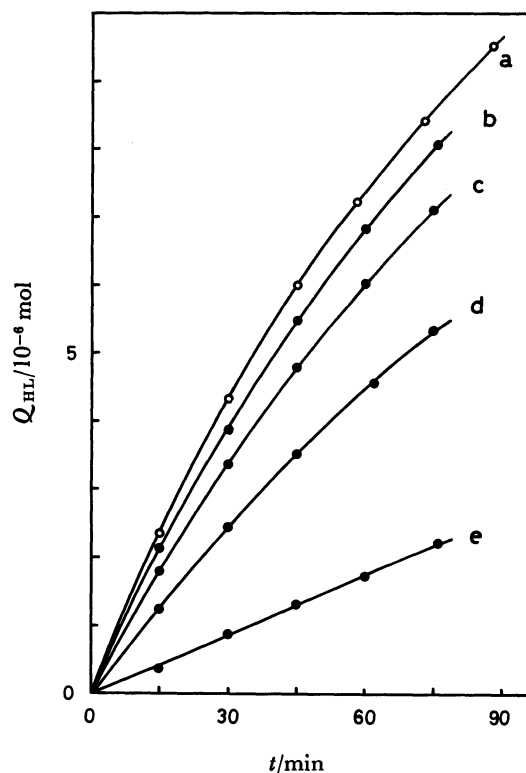


Fig. 4. The plots of  $Q_{HL}$  vs.  $t$  in the absence and presence of metal ions.  $N_2$  gas flow rate  $895 \text{ cm}^3 \text{ min}^{-1}$ ;  $C_{HL} = 5.85 \times 10^{-4} \text{ mol dm}^{-3}$ ; (a):  $C_M = 0$ , pH = 2.30, (b):  $C_{Mg} = 2.05 \times 10^{-3} \text{ mol dm}^{-3}$ , pH = 7.37, (c):  $C_{Ni} = 9.85 \times 10^{-3} \text{ mol dm}^{-3}$ , pH = 4.76, (d):  $C_{Cu}(\text{sulfate}) = 1.98 \times 10^{-3} \text{ mol dm}^{-3}$ , pH = 3.68, (e):  $C_{Fe(III)} = 4.02 \times 10^{-3} \text{ mol dm}^{-3}$ , pH = 1.82.

constant,  $k$  is proportional directly to the  $N_2$  gas flow rate in the range of  $250$  to  $895 \text{ cm}^3 \text{ min}^{-1}$  studied, as shown in Fig. 3. In the subsequent runs, the flow rate was fixed at  $895 \text{ cm}^3 \text{ min}^{-1}$  to reduce the time required for completing a single run.

**Estimation of  $K_1$ .** The amount of acetylacetone released into the gaseous phase was plotted against aeration time to give a parabolalike curve. Results for some metals are shown in Fig. 4, in which the result obtained in the absence of metal is included for comparison. Plots constructed with the aid of Eq. 8 gave straight lines for each run over the aeration time range investigated. Insofar as sample solutions are sufficiently acidic that the term  $K_a[H^+]^{-1}$  can be neglected compared to unity, and provided also that the total concentration of metal ions is sufficiently large compared with the ligand concentration, the slope of the straight line can be taken as  $-k/(1 + K_1 K_a C_M [H^+]^{-1})$ . The effect of  $C_M$  and pH on the slope was examined for Cu and Ni. The results are shown in Fig. 5 ( $C_{Ni} = 1.97 \times 10^{-3}$ – $4.93 \times 10^{-2} \text{ M}$ ,  $C_{HL} = 5.85 \times 10^{-4} \text{ M}$ , and pH almost constant around 4.8) and in Fig. 6 ( $C_{Cu} = 1.98 \times 10^{-3} \text{ M}$ ,  $C_{HL} = 5.85 \times 10^{-4} \text{ M}$ , and pH = 1.02–4.89). As expected, the gradient of the straight line decreases as either  $C_M$  or pH increases.

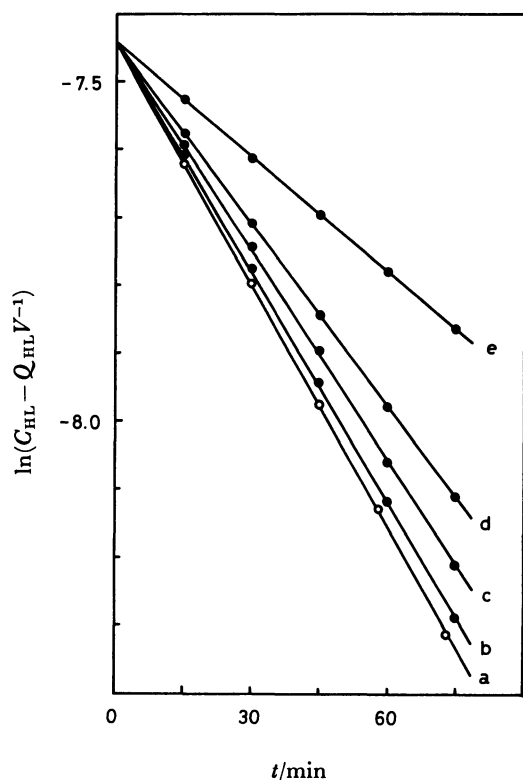


Fig. 5. The effect of  $C_M$  on the plots of  $\ln(C_{HL} - Q_{HL} V^{-1})$  vs.  $t$ .  $N_2$  gas flow rate  $895 \text{ cm}^3 \text{ min}^{-1}$ ;  $C_{HL} 5.85 \times 10^{-4} \text{ mol dm}^{-3}$ ; (a):  $C_M=0$ ,  $\text{pH}=2.30$ , (b):  $C_{Ni}=1.97 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $\text{pH}=4.80$ , (c):  $C_{Ni}=4.93 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $\text{pH}=4.80$ , (d):  $C_{Ni}=9.85 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $\text{pH}=4.80$ , (e):  $C_{Ni}=4.93 \times 10^{-2} \text{ mol dm}^{-3}$ ,  $\text{pH}=4.63$ .

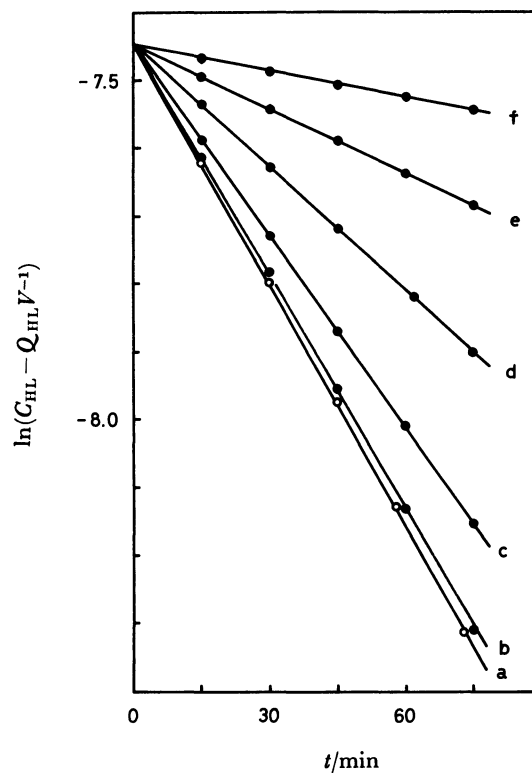


Fig. 6. The effect of  $\text{pH}$  on the plots of  $\ln(C_{HL} - Q_{HL} V^{-1})$  vs.  $t$ .  $N_2$  gas flow rate  $895 \text{ cm}^3 \text{ min}^{-1}$ ;  $C_{HL} 5.85 \times 10^{-4} \text{ mol dm}^{-3}$ ;  $C_{Cu}(\text{sulfate})$ : (a) 0, (b) — (f)  $1.98 \times 10^{-3} \text{ mol dm}^{-3}$ ;  $\text{pH}$ : (a) 2.30, (b) 1.02, (c) 3.00, (d) 3.68, (e) 4.28, (f) 4.89.

The  $k$  and  $K_a$  values being known from the runs undertaken in the absence of metal, we can evaluate  $K_1$  for each metal from the slope of the straight line. The  $K_1$  values thus determined for Cu and Ni under various  $C_M$  and  $\text{pH}$  conditions are given in Table 1, and those for the other seven metals studied are summarized in Table 2, in which the  $K_1$  values evaluated by using the reference  $\text{p}K_a(=8.82)$  are also listed together with those reported in the literature.<sup>4-8)</sup> The  $K_1$  values obtained by the present method are in reasonable agreement within 0.1 to 0.2 in the log unit with the literature values except for Al(III), which case differs by ca. 0.4 log unit.

### Discussion

There are various factors which affect the precision and accuracy of the method proposed here for evaluating association constants between volatile and nonvolatile solutes. As was noted in a previous paper,<sup>1)</sup> it is a requirement to carry out two separate runs, one in the absence and the other in the presence of nonvolatile solutes, under the same aeration conditions. To meet this requirement, the same sintered glass ball should be used in common, and the  $N_2$  gas

flow rate should be controlled to be as identical with each other as possible. Indeed, the rate constant,  $k$ , the absolute value of which is of no significance, is a function of the aeration rate (Fig. 3). In addition, the ionic strength and the kind of the electrolyte used to adjust it should be the same for the two runs, because the so-called salting-out effect may influence the volatility of the solute of interest, and hence the  $k$  value.

Particular attention should be paid to the presence of such electrolytes as may cause association with the nonvolatile solute to be studied, since this also affects the accuracy of the present method. For instance, the  $K_1$  value for Cu decreases step by step as  $C_M$  increases, as can be seen from Table 1, when the sulfate salt is used; we first thought this arose from the salting-out of  $\text{SO}_4^{2-}$  ions, but it now seems more reasonable to consider ion-pair formation between  $\text{Cu}^{2+}$  and  $\text{SO}_4^{2-}$ .<sup>10)</sup> The  $K_1$  value of Cu(II) for the chloride salt is employed for this reason. Incidentally, the ion-pair formation constant has been reported to be ca. 200 at  $25^\circ\text{C}$  and at ionic strengths corrected to zero.<sup>3)</sup> The  $K_1$  value of Cu(II) for the sulfate salt is to be underestimated unless the free metal ion concentration,  $[\text{M}^{n+}]$ , in the experimentally determined slope,  $-k/(1+K_1K_a[\text{M}^{n+}][\text{H}^+]^{-1})$ , is corrected for the

Table 1. Effects of the Total Concentration of Metal Ion and pH of Aqueous Solution on the Estimation of Formation Constants of Cu(II) and Ni(II) Acetylacetonate Complexes<sup>a)</sup>

Metal ion <sup>b)</sup>	$10^3 \times C_M / \text{mol dm}^{-3}$	pH	$\log K_1^c)$
Cu(II), $\text{SO}_4^{2-}$	1.98	3.00	8.3
	4.96	3.00	8.2
	9.92	3.00	8.2
	49.6	3.08	8.0
	1.98	1.02	9.4 <sup>d)</sup>
	1.98	3.68	8.2
	1.98	4.28	8.0
Cu(II), $\text{Cl}^-$	1.98	4.89	7.9
	1.96	2.92	8.3
	4.90	2.88	8.3
	9.80	2.85	8.2
Ni(II), $\text{Cl}^-$	49.0	2.79	8.2
	1.97	4.80	5.9
	4.93	4.80	5.9
	9.85	4.76	6.0
	49.3	4.63	5.9
	1.97	3.80	6.5 <sup>d)</sup>
	1.97	5.56	5.9
	1.97	6.36	5.7

a) The total concentration of acetylacetone is  $5.85 \times 10^{-4} \text{ mol dm}^{-3}$ , temperature is  $25.0 \pm 0.1^\circ \text{C}$ , and  $I=0.1$  ( $\text{NaClO}_4$ ). b) The counter anion is specified. c) Estimated with  $\text{p}K_a=9.17$ . d) See the text.

Table 2. Formation Constants,  $K_1$ , of Metal Acetylacetonates at  $25.0 \pm 0.1^\circ \text{C}$  and  $I=0.1$  ( $\text{NaClO}_4$ )

Metal ion <sup>a)</sup>	$10^3 \times C_M / \text{mol dm}^{-3}$	pH	$\log K_1$	
			This work <sup>b)</sup>	Literature
Cu(II)	1.96— 49.0	2.79— 2.92	8.3 (7.9) <sup>e)</sup>	8.16 <sup>d)</sup>
Ni(II)	1.97— 49.3	4.63— 6.36	5.9 (5.5) <sup>e)</sup>	5.72 <sup>d)</sup>
Co(II)	2.02	5.58	5.3 (5.0)	5.10 <sup>e)</sup>
Mg(II)	2.05	7.37	3.5 (3.1)	3.34 <sup>e)</sup>
Fe(II)	6.44	5.30	5.2 (4.9)	5.07 <sup>f)</sup>
Fe(III)	4.02	1.82	10.5 (10.2)	9.27 <sup>g)</sup> , 10.5 <sup>h)</sup>
Al(III)	4.98	2.00	8.7 (8.3)	8.25 <sup>g)</sup>

a) Chloride salt except for Fe(III) (ammonium iron(III) sulfate) and Al(III) (aluminium potassium sulfate).

b) The total concentration of acetylacetone is  $5.85 \times 10^{-4} \text{ mol dm}^{-3}$ , and the value are derived based on  $\text{p}K_a=9.17$  estimated in this work, those on  $\text{p}K_a=8.82$  (the literature value, Ref. 9) being given in the parentheses.

c) The average of the chloride salts given in Table 1 (the value for Ni with the superscript d in Table 1 is excluded). d) Ref. 4,  $25^\circ \text{C}$ ,  $I=0.1$  ( $\text{NaClO}_4$ ). e) Recommended values cited in Ref. 5,  $25^\circ \text{C}$ ,  $I=0.1$  ( $\text{Na}^+$ ,  $\text{H}^+$ )  $\text{ClO}_4^-$ . f) Ref. 6,  $30^\circ \text{C}$ ,  $I=0$ . g) Ref. 7,  $25^\circ \text{C}$ , low ionic strength. h) Ref. 8,  $25^\circ \text{C}$ ,  $I=1.0$ .

ion-pair formation, that is,  $[\text{Cu}^{2+}] = C_{\text{Cu}} - [\text{Cu}^{2+}\text{SO}_4^{2-}]$ .

The choice of proper  $\text{p}K_a$  value is essential in estimating  $K_1$ . We have listed the two  $K_1$  values in Table 2, one being evaluated based on  $\text{p}K_a=9.17$  and the other on  $\text{p}K_a=8.82$  reported in the literature. Although the  $K_a$  value determined in this work is appreciably lower, we are of the opinion that the use of this value leads to a better  $K_1$  value since the same procedure employed to evaluate both  $\text{p}K_a$  and  $K_1$  tends to compensate for systematic errors inherent in the present method.

An important point to keep in mind is the magnitude of the product,  $K_1 K_a C_M [\text{H}^+]^{-1}$ . The value of  $K_1$ , cannot be evaluated accurately or at all when the term is too small compared with unity. This may be responsible for the unusual values observed for Cu at  $\text{pH}=1.02$  and for Ni at  $\text{pH}=3.80$  (Table 1). To get more reliable  $K_1$ , the solution pH and/or  $C_M$  should desirably be high for metals with relatively small stability constants. The choice of the solution pH, however, may be limited for metals subject to hydrolysis. For metals with large stability constants, on the other hand, these conditions are not necessarily desirable, because it takes a prolonged time to expel the free ligand from the aqueous phase.

When it is necessary to consider hydrolysis of metal ions, the concentration of  $\text{M}^{n+}$  should be modified by using  $\alpha_{\text{M(OH)}}$ , a side reaction coefficient, into  $[\text{M}^{n+}] = C_M / \alpha_{\text{M(OH)}}$ ; with correction for the hydrolysis reaction,  $\text{M}^{n+} + \text{H}_2\text{O} \rightleftharpoons \text{M(OH)}^{n-1} + \text{H}^+$ , the complex formation constant,  $K_{1,\text{correct}}$ , can be written as

$$\log K_{1,\text{correct}} = \log K_1 + \log \alpha_{\text{M(OH)}},$$

including the second term of the right hand side of the equation as a correction term. This correction term, however, is negligibly small at the solution pH adopted here except for Fe(III). The  $K_1$  value of Fe(III) listed in Table 2 has been corrected by 0.1 in the logarithmic unit; for Fe(III) the literature value of  $-2.55$  was used as  $\log K_{\text{hydrolysis}}$ , where  $K_{\text{hydrolysis}}$  is the hydrolysis constant and can be converted into the side reaction coefficient by the relationship,  $\alpha_{\text{M(OH)}} = 1 + K_{\text{hydrolysis}} [\text{H}^+]^{-1}$ .

An attempt was made to evaluate 1:2 formation constants for some metal acetylacetonato complexes on the basis of the equilibration



It is difficult in this case to derive a rate equation like Eq. 7 under the experimental condition  $C_{\text{HL}} > C_M$  or  $C_{\text{HL}} \approx C_M$ . We therefore tried to estimate  $K_2$  through the following three successive steps. The first step:  $\log(Q_{\text{HL}}/V)$  is plotted vs.  $\log t$  to give a straight line for each run, and the intercept,  $\log a$ , and the slope,  $b$ , are derived. The second step: on the assumption  $Q_{\text{HL}}/V = a t^b$ ,  $dQ_{\text{HL}}/dt$  is calculated at a selected aeration time,  $t$ , and then, the concentration of free

HL present in the solution at  $t$  is obtained based on the rate equation, Eq. 4. The third step: from the mass-balance equations

$$C_{HL} = [HL] + Q_{HL}/V + [L^-] + [ML^{n-1}] + 2[ML_2^{n-2}],$$

$$C_M = [M^{n+}] + [ML^{n-1}] + [ML_2^{n-2}],$$

Table 3. Change in Concentration of Free Ligand and Metal Complexes as a Function of Aeration Time and the Tentatively Estimated Formation Constants,  $K_2$ , of Metal Acetylacetonates at  $25.0 \pm 0.1^\circ \text{C}$ ,  $I=0.1(\text{NaClO}_4)$

Aeration time/min	Concentration/ $10^{-4}$ mol dm $^{-3}$					$\log K_2$
	$Q_{HL}/V$	HL	M $^{n+}$	ML $^{n-1}$	ML $_2^{n-2}$	
Cu(II) <sup>a)</sup>						
15	1.71	8.26	0.83	6.51	2.46	6.9
30	3.23	7.45	0.98	6.92	1.90	6.9
45	4.53	7.01	1.13	7.49	1.19	6.6
60.5	5.73	6.71	1.27	8.10	0.43	6.2
76.5	6.77	6.49	1.41	8.65		
				Average		6.7
				Literature value <sup>b)</sup>		6.84
Ni(II) <sup>c)</sup>						
15	1.89	9.12	1.77	5.82	2.26	4.9
30	3.54	8.25	2.04	6.06	1.76	4.9
45	4.99	7.78	2.31	6.49	1.05	4.7
60	6.29	7.47	2.58	6.94	0.33	4.1
75	7.45	7.23	2.82	7.37		
				Average		4.8
				Literature value <sup>d)</sup>		4.45
Fe(III) <sup>e)</sup>						
15	2.25	11.08	6.43	20.08	11.31	9.7
30	4.28	10.01	6.96	19.63	11.03	9.7
45	6.09	9.43	7.40	19.66	10.40	9.7
60	7.83	9.03	7.80	10.85	9.67	9.7
75	9.43	8.74	8.15	20.07	8.96	9.7
90	10.93	8.51	8.49	20.36	8.21	9.7
				Average		9.7
				Literature value <sup>b)</sup>		8.71
Al(III) <sup>f)</sup>						
15	2.11	10.02	3.27	4.11	2.58	8.4
30	3.97	8.95	3.67	4.11	2.19	8.4
45	5.53	8.37	4.07	4.27	1.16	8.3
60	6.85	7.98	4.45	4.45	1.06	8.1
75	8.06	7.70	4.82	4.64	0.50	7.7
				Average		8.2
				Literature value <sup>b)</sup>		7.35

a) As the chloride salt,  $C_{Cu}=9.80 \times 10^{-4} \text{ mol dm}^{-3}$ ,  $C_{HL}=2.14 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $\text{pH}=4.89$ , and the data used are  $\text{p}K_a=9.17$  and  $\log K_1=8.3$ . b) Ref. 7. c)  $C_{Ni}=9.85 \times 10^{-4} \text{ mol dm}^{-3}$ ,  $C_{HL}=2.14 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $\text{pH}=6.86$ , and the data used are  $\text{p}K_a=9.17$  and  $\log K_1=5.9$ . d) Ref. 5. e)  $C_{Fe}=4.02 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $C_{HL}=4.87 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $\text{pH}=2.12$ , and the data used are  $\text{p}K_a=9.17$  and  $\log K_1=10.5$ . f)  $C_{Al}=9.96 \times 10^{-4} \text{ mol dm}^{-3}$ ,  $C_{HL}=2.14 \times 10^{-3} \text{ mol dm}^{-3}$ ,  $\text{pH}=3.58$ , and the data used are  $\text{p}K_a=9.17$  and  $\log K_1=9.7$ .

we can derive

$$C_{HL} = [HL] + Q_{HL}/V + K_a[HL][H^+]^{-1} + 2C_M - [M^{n+}](2 + K_1K_a[HL][H^+]^{-1}),$$

which allows us to estimate  $[M^{n+}]$  by using the  $K_a$  and  $K_1$  values evaluated by the present method, and in turn,  $[ML^{n-1}]$  and  $[ML_2^{n-2}]$  can be determined from the mass-balance relationships, from which  $K_2$  is to be derived. The values thus determined are given in Table 3. Again, if it is necessary to make correction for the hydrolysis of metal ions, the product  $[M^{n+}]\alpha_{M(OH)}$  must be employed instead of the simple  $[M^{n+}]$ ; this correction was applied only to Fe(III).

It is informative to follow the change in concentration of such species as  $M^{n+}$ ,  $ML^{n-1}$ , and  $ML_2^{n-2}$  as a function of aeration time. As aeration proceeds,  $[ML_2^{n-2}]$  decreases with an accompanying increase in  $[M^{n+}]$  (and also in  $[ML^{n-1}]$  when  $C_{HL}$  is sufficiently large compared to  $C_M$ ). In the case of Fe(III) given in Table 3, there was observed a steady state with respect to the  $ML^{n-1}$  species, which may result from  $C_{HL}$  being nearly equal to  $C_M$ . It appears that the  $K_2$  value thus derived for each metal falls gradually as aeration proceeds. This is quite unreasonable and is probably caused by the assumption made in the second step, that is, the  $Q_{HL}/V$  vs.  $t$  plot follows a parabolic curve. In reality, the  $\log(Q_{HL}/V)$  vs.  $\log t$  plots show a slight deviation from the linearity and this trend is pronounced with prolonging aeration time. Therefore, the differential treatment of experimental results employed here to estimate  $K_2$  led to erroneous evaluation of 1:2 association constants.

If it is convenient to follow the rate of decrease in the concentration of the associated species instead of measuring the releasing rate of the volatile solute expelled from the aqueous into the gaseous phase, the rate equation can be expressed as

$$-d[A \cdot B]/dt = kK^{-1}[A \cdot B][B]^{-1} = kK^{-1}[A \cdot B](C_M - [A \cdot B])^{-1},$$

which becomes, on integration and with  $[A \cdot B] = [A \cdot B]_0$ , the initial ( $t=0$ ) concentration

$$C_B \ln [A \cdot B] - [A \cdot B] = -kK^{-1}t + C_B \ln [A \cdot B]_0 - [A \cdot B]_0,$$

where A, B, and A·B denote the volatile, nonvolatile, and associated species, respectively,  $K$  is an association constant, and  $k$  is a rate constant of the expulsion of A from the aqueous phase in the absence of B. This is essentially the same form as that previously used to determine the disproportionation constant of mercury(I).<sup>1)</sup> Implicit in this rate equation and also in Eq. 4 (and Eq. 7) is the assumption that the transfer of volatile solute from

the aqueous into the gaseous phase is the rate-determining step. If, on the other hand, an association equilibrium is the rate-determining step, the association constant cannot be estimated. This is a limitation on the applicability of the present method.

In general, it is somewhat difficult to measure association constants between nonvolatile and highly volatile solutes, because it is hard to maintain constant the concentration of the latter in the aqueous medium. The present method is applicable only to very volatile solutes, and in this respect seems complementary. The present technique need not maintain the volatile solute concentration constant, and its total concentration in the aqueous medium can easily be determined by aerating the medium with an inert gas for a prolonged period and by trapping the released solute during the aeration.

An important application of the method proposed here will be encountered when hydrophobic interaction is to be studied in the aqueous environment between nonvolatile and volatile solutes.

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